

58. We neglect air resistance, which justifies setting  $a = -g = -9.8 \text{ m/s}^2$  (taking *down* as the  $-y$  direction) for the duration of the motion. We are allowed to use Table 2-1 (with  $\Delta y$  replacing  $\Delta x$ ) because this is constant acceleration motion. When something is thrown straight up and is caught at the level it was thrown from (with a trajectory similar to that shown in Fig. 2-25), the time of flight  $t$  is half of its time of ascent  $t_a$ , which is given by Eq. 2-18 with  $\Delta y = H$  and  $v = 0$  (indicating the maximum point).

$$H = vt_a + \frac{1}{2}gt_a^2 \implies t_a = \sqrt{\frac{2H}{g}}$$

Writing these in terms of the total time in the air  $t = 2t_a$  we have

$$H = \frac{1}{8}gt^2 \implies t = 2\sqrt{\frac{2H}{g}}.$$

We consider two throws, one to height  $H_1$  for total time  $t_1$  and another to height  $H_2$  for total time  $t_2$ , and we set up a ratio:

$$\frac{H_2}{H_1} = \frac{\frac{1}{8}gt_2^2}{\frac{1}{8}gt_1^2} = \left(\frac{t_2}{t_1}\right)^2$$

from which we conclude that if  $t_2 = 2t_1$  (as is required by the problem) then  $H_2 = 2^2H_1 = 4H_1$ .